

Causal mediation analysis using Stata

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May 9, 2024

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Causal inference and mediation

- The goal of causal inference is to identify and quantify the effect of some treatment (exposure) on some outcome.
- With causal mediation, we can disentangle causal effects into direct and indirect effects.
- By decomposing causal effects into direct and indirect effects, we are targeting the underlying mechanism of causal relations.
- In other words, we use causal mediation to learn about *why* certain causes have the effect they have.

Causal diagram illustration

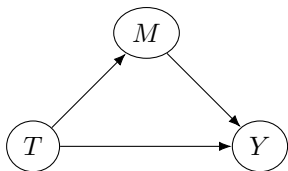
- Simple causal model for the effect of T on Y :



- Causal model for the effect of T on Y through M :



- Mediation model with a direct and an indirect effect:



Potential outcomes framework (1)

- Consider a simple randomized experiment with binary treatment T and outcome Y , with sample observations $i = 1 \dots N$.
- We wish to identify two sets of potential outcomes, $Y_i(1)$ and $Y_i(0)$, where $Y_i(t)$ is the outcome that would be realized if the i th individual were exposed to treatment level t .
- If it were possible to observe an individual in both states at the same time, we would observe one outcome value under treatment, $Y_i(1)$, and one value under the control condition, $Y_i(0)$.
- The (individual-level) treatment effect would then be the difference $\tau_i = Y_i(1) - Y_i(0)$.
- Averaging the difference over all individuals in the sample would yield an estimate of the ATE
$$\tau = E[Y_i(1) - Y_i(0)] = E[Y_i(1)] - E[Y_i(0)].$$

Potential outcomes framework (2)

- As we know, it is not possible to observe the same individual under both conditions at the same time.
- We can only observe one of these while the other is missing.
- If an individual is treated, we observe $Y_i(1)$, and if not, we observe $Y_i(0)$.
- This has been coined the “fundamental problem of causal inference”
- Much of the treatment effects and causal inference literature deals with the question of how to estimate an ATE in the presence of this problem.
- In a simple experiment where treatment is randomly assigned, the potential outcomes are independent of treatment assignment and the missing potential outcomes are missing completely at random.
- With observational rather than experimental data the potential outcomes are not independent of the treatment assignment process, and the causal effect is not identifiable without imposing further assumptions such as conditional independence.

Potential outcome framework for causal mediation

- Now consider the case where we have a mediator M in addition to treatment T and outcome Y .
- We now have an additional set of potential outcomes, $M_i(1)$ and $M_i(0)$, because M is also causally related to the treatment.
- $M_i(1)$ are the potential outcomes of the mediator that would be observed had the i th individual been assigned to the group of active treatment.
- $M_i(0)$ are the potential outcomes of the mediator that would be observed had the i th individual been assigned to the control group.
- Let t be the treatment level with respect to the outcome, and let t' be the treatment level with respect to the mediator, the potential outcomes become $Y_i[t, M_i(t')]$.

Causal mediation potential outcomes (1)

- With binary treatment, we now have four sets of potential outcomes: $Y_i[0, M_i(0)]$, $Y_i[1, M_i(1)]$, $Y_i[1, M_i(0)]$ and $Y_i[0, M_i(1)]$.
- $Y_i[0, M_i(0)]$ is observed if $T_i = 0$.
- $Y_i[1, M_i(1)]$ is observed if $T_i = 1$.
- $Y_i[0, M_i(0)]$ are the potential outcomes that we would observe if nobody in the population received treatment.
- $Y_i[1, M_i(1)]$ are the potential outcomes that we would observe if everybody in the population received treatment.
- Notice that $Y_i[0, M_i(0)] = Y_i(0)$ and $Y_i[1, M_i(1)] = Y_i(1)$

Causal mediation potential outcomes (2)

- $Y_i[1, M_i(0)]$ and $Y_i[0, M_i(1)]$, sometimes referred to as cross-world potential outcomes, are never observed.
- $Y_i[1, M_i(0)]$ are the potential outcomes that we would observe if everybody in the population received treatment, but where the mediator is held at a value that would be observed as though nobody in the population received treatment.
- $Y_i[0, M_i(1)]$ are the potential outcomes that we would observe if nobody in the population received treatment, but where the mediator is held at a value that would be observed as though everybody in the population received treatment.

Direct, indirect, and total treatment effects

- Average direct, indirect, and total treatment effects are contrasts between potential outcome means.

- The total effect is:

$$\tau \equiv E[Y_i(1)] - E[Y_i(0)] = E[Y_i(1, M_i(1))] - E[Y_i(0, M_i(0))]$$

- The effect of the treatment on the outcome through the mediator is the indirect effect:

$$\delta(t) \equiv E[Y_i(t, M_i(1))] - E[Y_i(t, M_i(0))], \quad t \in \{0, 1\}$$

- The direct effect of the treatment is:

$$\zeta(t) \equiv E[Y_i(1, M_i(t))] - E[Y_i(0, M_i(t))], \quad t \in \{0, 1\}$$

- Notice that the total effect is the sum of direct and indirect effects

$$\tau = \delta(t) + \zeta(t)$$

Two treatment effect decompositions

- If we include a treatment-mediator interaction, the total treatment effect can be decomposed in two different ways.
- We can decompose the total effect using components $\delta(0) \equiv E[Y_i(0, M_i(1))] - E[Y_i(0, M_i(0))]$ and $\zeta(0) \equiv E[Y_i(1, M_i(0))] - E[Y_i(0, M_i(0))]$
- ... as well as $\delta(1) \equiv E[Y_i(1, M_i(1))] - E[Y_i(1, M_i(0))]$ and $\zeta(1) \equiv E[Y_i(1, M_i(1))] - E[Y_i(0, M_i(1))]$
- If we do not include a treatment-mediator interaction, i.e., we impose the assumption that the effect of the mediator on the outcome does not vary across treatment groups, we have that $\delta(0) = \delta(1)$ and $\zeta(0) = \zeta(1)$.

Estimands

- Denoting $E[Y_i(t, M_i(t'))]$ as $Y_{tM_t'}$, we define the following treatment effects of interest

(Total) natural indirect effect (NIE)	$Y_{1M_1} - Y_{1M_0}$
(Pure) natural direct effect (NDE)	$Y_{1M_0} - Y_{0M_0}$
(Pure) natural indirect effect (PNIE)	$Y_{0M_1} - Y_{0M_0}$
(Total) natural direct effect (TNDE)	$Y_{1M_1} - Y_{0M_1}$
Total effect (TE)	$Y_{1M_1} - Y_{0M_0}$

How to identify potential outcome means?

- The potential-outcome means are the result of an integral of the conditional expectation of the outcome with respect to the conditional distribution of the mediator:

$$f[Y_i(t, M_i(t')) | \mathbf{X}_i = \mathbf{x}] = \int f[Y_i | M_i = m, T_i = t, \mathbf{X}_i = \mathbf{x}] dF[m | T_i = t', \mathbf{X}_i = \mathbf{x}]$$

- This is sometimes referred to as the "mediation formula".
- It expresses the potential outcomes as a function of the conditional distribution of M_i given T_i and \mathbf{X}_i , and that of Y_i given M_i , T_i , and \mathbf{X}_i .
- Notice that this is a nonparametric identification result.

Illustrative example using a linear model (1)

- Suppose we have the following model with two equations:

$$Y_i = \beta_0 + \beta_1 M_i + \beta_2 T_i + \epsilon_i$$

$$M_i = \alpha_0 + \alpha_1 T_i + \nu_i$$

- To calculate the natural indirect effect (NIE), we need estimates for potential-outcome means $E[Y_i(1, M_i(1))]$ and $E[Y_i(1, M_i(0))]$.
- With the linear model, we can write the model in reduced form and yield the conditional expectation of outcome Y :

$$\begin{aligned} E[Y_i | M_i, T_i] &= \beta_0 + \beta_1(\alpha_0 + \alpha_1 T_i) + \beta_2 T_i \\ &= \beta_0 + \beta_1 \alpha_0 + \beta_1 \alpha_1 T_i + \beta_2 T_i \end{aligned}$$

- To obtain the potential-outcome means, we can modify the reduced-form model by replacing M_i with the expectation of M_i that we would observe if T_i had taken on the value t' for every unit in the population:

$$E[Y_i(t, M_i(t'))] = \beta_0 + \beta_1 E[M_i(t')] + \beta_2 t, \quad t \in \{0, 1\}$$

Illustrative example using a linear model (2)

- Now, to compute the potential-outcome mean $E[Y_i(1, M_i(1))]$, we must set the treatment T_i to 1 in both the outcome and the mediator equations. In other words, we fix both t and t' at 1:

$$\begin{aligned} E[Y_i(1, M_i(1))] &= \beta_0 + \beta_1 E[M_i(t')] + \beta_2 t, \quad t = t' = 1 \\ &= \beta_0 + \beta_1 \alpha_0 + \beta_1 \alpha_1 \times 1 + \beta_2 \times 1 \\ &= \beta_0 + \beta_1 \alpha_0 + \beta_1 \alpha_1 + \beta_2 \end{aligned}$$

- To compute $E[Y_i(1, M_i(0))]$, we need to set treatment T_i to 1 in the outcome equation but set it to 0 in the mediator equation. Specifically, we fix $t' = 0$ and $t = 1$:

$$\begin{aligned} E[Y_i(1, M_i(0))] &= \beta_0 + \beta_1 E[M_i(t')] + \beta_2 t, \quad t = 1; t' = 0 \\ &= \beta_0 + \beta_1 \alpha_0 + \beta_1 \alpha_1 \times 0 + \beta_2 \times 1 \\ &= \beta_0 + \beta_1 \alpha_0 + \beta_2 \end{aligned}$$

Illustrative example using a linear model (3)

- Calculating the difference yields the indirect treatment effect

$$\begin{aligned}\delta(1) &= (\beta_0 + \beta_1\alpha_0 + \beta_1\alpha_1 + \beta_2) - (\beta_0 + \beta_1\alpha_0 + \beta_2) \\ &= \beta_0 + \beta_1\alpha_0 + \beta_1\alpha_1 + \beta_2 - \beta_0 - \beta_1\alpha_0 - \beta_2 \\ &= \beta_1\alpha_1\end{aligned}$$

- We are left with the product of the treatment coefficient from the mediator equation and the mediator coefficient from the outcome equation.
- This is congruent with the classical product-of-coefficients method.
- Had we included a treatment-mediator interaction, the result would be $\delta(1) = (\beta_1 + \beta_3)\alpha_1$.
- Not as simple for models other than the linear model.

Assumptions for identifying estimands of interest

- SUTVA, overlap, **sequential ignorability**
- Sequential ignorability essentially means
 - ▶ No unobserved confounding in the treatment-outcome relationship.
 - ▶ No unobserved confounding in the mediator-outcome relationship.
 - ▶ No unmeasured confounding in the treatment-mediator relationship.
 - ▶ There are no (observed) confounders in the mediator-outcome relationship that are caused by the treatment.

Stata's `mediate` command

- New in Stata 18: `mediate`
- `mediate` performs causal mediation analysis for linear and generalized linear models.
- It uses analytical expressions to compute potential outcome means based on parametric models.
- Outcome and mediator variables may be continuous, binary, or count.
- Treatment may be binary, multivalued, or continuous.
- Linear, logit, probit, Poisson, and exponential-mean models for outcome and mediator.
- Special-purpose postestimation commands.

Outcome and mediator model combinations

	linear	logit	probit	Poisson	exp. mean
linear	x	x	x	x	x
logit		x	x	x	
probit	x	x	x	x	x
Poisson	x	x	x	x	x
exp. mean	x	x	x	x	x

Note: x indicates supported model combination

Postestimation commands

- Special-purpose postestimation commands include

- ▶ `estat proportion` proportion mediated
- ▶ `estat cde` controlled direct effects
- ▶ `estat rr` treatment effects as risk ratios
- ▶ `estat or` treatment effects as odds ratios
- ▶ `estat irr` treatment effects as incidence-rate ratios
- ▶ `estat effectsplot` plot treatment effects

Treatment effects on different scales (1)

- If the outcome is binary, and if the outcome model is either `logit` or `probit`, we can express the treatment effects as risk ratios or odds ratios.
- If the outcome model is Poisson/exponential mean, treatment effects can be expressed as incidence-rate ratios.
- The treatment effects on risk-ratio and incidence-rate-ratio scales are ratios of potential-outcome means:

$$\text{NIE}^{\text{RR}} \equiv Y_{1M_1} / Y_{1M_0}$$

$$\text{NDE}^{\text{RR}} \equiv Y_{1M_0} / Y_{0M_0}$$

$$\text{PNIE}^{\text{RR}} \equiv Y_{0M_1} / Y_{0M_0}$$

$$\text{TNDE}^{\text{RR}} \equiv Y_{1M_1} / Y_{0M_1}$$

$$\text{TE}^{\text{RR}} \equiv Y_{1M_1} / Y_{0M_0}$$

Treatment effects on different scales (2)

- For logit and probit outcome models, Y_{tM_t} are probabilities, and so the treatment effects on odds-ratio scale are

$$\text{NIE}^{\text{OR}} \equiv Y_{1M_1}/(1 - Y_{1M_1})/\{Y_{1M_0}/(1 - Y_{1M_0})\}$$

$$\text{NDE}^{\text{OR}} \equiv Y_{1M_0}/(1 - Y_{1M_0})/\{Y_{0M_0}/(1 - Y_{0M_0})\}$$

$$\text{PNIE}^{\text{OR}} \equiv Y_{0M_1}/(1 - Y_{0M_1})/\{Y_{0M_0}/(1 - Y_{0M_0})\}$$

$$\text{TNDE}^{\text{OR}} \equiv Y_{1M_1}/(1 - Y_{1M_1})/\{Y_{0M_1}/(1 - Y_{0M_1})\}$$

$$\text{TE}^{\text{OR}} \equiv Y_{1M_1}/(1 - Y_{1M_1})/\{Y_{0M_0}/(1 - Y_{0M_0})\}$$

- Notice that for all of these scales, the decomposition becomes multiplicative; that is, the total effect becomes the product of direct and indirect effects.

Controlled direct effects

- A controlled direct effect (CDE) is the effect of a treatment on an outcome when the mediator is fixed at a particular value.
- To estimate controlled direct effects, we use only the results of the outcome equation.
- Rather than having potential outcomes of the form $Y_i(t, M_i(t'))$, here we have potential outcomes $Y_i(t|M_i = m)$.
- That is, we have potential outcomes for each treatment level t that are evaluated at value m of the mediator.
- CDE(m) is then the average of the differences between potential outcomes.
- For binary treatment, CDE(m) is defined as $Y_i(1|M_i = m) - Y_i(0|M_i = m)$.
- Letting Y_{tm} be a shorthand for $Y_i(t|M_i = m)$, we have that

$$\text{CDE}(m) \equiv Y_{1m} - Y_{0m}$$

$$\text{CDE}(m)^{\text{RR}} \equiv Y_{1m}/Y_{0m}$$

$$\text{CDE}(m)^{\text{IRR}} \equiv Y_{1m}/Y_{0m}$$

$$\text{CDE}(m)^{\text{OR}} \equiv Y_{1m}/(1 - Y_{1m})/\{Y_{0m}/(1 - Y_{0m})\}$$

Example data (1)

```
. webuse wellbeing
(Fictional well-being data)

. list wellbeing bonotonin exercise age gender in 1/5, abbreviate(12) clean
```

	wellbeing	bonotonin	exercise	age	gender
1.	71.73816	196.5467	Control	58	Male
2.	68.66573	195.8572	Exercise	38	Female
3.	71.05155	228.6035	Exercise	53	Female
4.	69.44469	206.6651	Exercise	44	Female
5.	75.62035	261.6855	Exercise	28	Female

Linear models with no treatment-mediator interaction

```
. mediate (wellbeing) (bonotonin) (exercise), nointeraction
```

```
Iteration 0: EE criterion = 6.800e-28
```

```
Iteration 1: EE criterion = 1.777e-28
```

```
Causal mediation analysis
```

```
Number of obs = 2,000
```

```
Outcome model: Linear
```

```
Mediator model: Linear
```

```
Mediator variable: bonotonin
```

```
Treatment type: Binary
```

wellbeing	Coefficient	Robust std. err.	z	P> z	[95% conf. interval]	
NIE						
exercise (Exercise vs Control)	9.694617	.377312	25.69	0.000	8.955099	10.43413
NDE						
exercise (Exercise vs Control)	2.996658	.2109357	14.21	0.000	2.583231	3.410084
TE						
exercise (Exercise vs Control)	12.69127	.4005769	31.68	0.000	11.90616	13.47639

```
Note: Outcome equation does not include treatment-mediator interaction.
```


Proportion mediated

```
. estat proportion
```

```
Proportion mediated
```

```
Number of obs = 2,000
```

wellbeing	Proportion	Robust std. err.	z	P> z	[95% conf. interval]	
exercise (Exercise vs Control)	.7638805	.0154928	49.31	0.000	.7335151	.7942459

Linear models with treatment-mediator interaction

```
. mediate (wellbeing basewell age gender hstatus)    ///  
>          (bonotonin basebono age gender hstatus)  ///  
>          (exercise)
```

Iteration 0: EE criterion = 2.004e-27

Iteration 1: EE criterion = 2.804e-28

Causal mediation analysis

Number of obs = 2,000

Outcome model: Linear

Mediator model: Linear

Mediator variable: bonotonin

Treatment type: Binary

wellbeing	Robust				[95% conf. interval]	
	Coefficient	std. err.	z	P> z		
NIE						
exercise (Exercise vs Control)	10.02204	.2256812	44.41	0.000	9.579717	10.46437
NDE						
exercise (Exercise vs Control)	3.085412	.168631	18.30	0.000	2.754901	3.415922
TE						
exercise (Exercise vs Control)	13.10746	.2304752	56.87	0.000	12.65573	13.55918

Note: Outcome equation includes treatment-mediator interaction.

Estimating potential outcome means

```
. mediate (wellbeing basewell age gender hstatus)    ///  
>          (bonotonin basebono age gender hstatus)  ///  
>          (exercise), pom
```

Iteration 0: EE criterion = 2.050e-27

Iteration 1: EE criterion = 2.775e-28

Causal mediation analysis

Number of obs = 2,000

Outcome model: Linear
Mediator model: Linear
Mediator variable: bonotonin
Treatment type: Binary

wellbeing	Robust					[95% conf. interval]	
	Coefficient	std. err.	z	P> z			
PMeans							
YOM0	56.89975	.228515	249.00	0.000	56.45187	57.34763	
Y1M0	59.98516	.2555341	234.74	0.000	59.48432	60.486	
YOM1	66.83246	.2644294	252.74	0.000	66.31419	67.35073	
Y1M1	70.0072	.2314185	302.51	0.000	69.55363	70.46077	

Note: Outcome equation includes treatment-mediator interaction.

Estimating all effects and potential outcome means

```
. mediate (wellbeing basewell age gender hstatus)      ///
>         (bonotonin basebono age gender hstatus)    ///
>         (exercise), all

Iteration 0: EE criterion = 2.132e-27
Iteration 1: EE criterion = 3.527e-28

Causal mediation analysis                          Number of obs = 2,000
Outcome model:   Linear
Mediator model:  Linear
Mediator variable: bonotonin
Treatment type:  Binary
```

wellbeing	Coefficient	Robust std. err.	z	P> z	[95% conf. interval]	
PMeans						
Y0M0	56.89975	.228515	249.00	0.000	56.45187	57.34763
Y1M0	59.98516	.2555341	234.74	0.000	59.48432	60.486
Y0M1	66.83246	.2644294	252.74	0.000	66.31419	67.35073
Y1M1	70.0072	.2314185	302.51	0.000	69.55363	70.46077
NIE						
exercise (Exercise vs Control)	10.02204	.2256812	44.41	0.000	9.579717	10.46437
NDE						
exercise (Exercise vs Control)	3.085412	.168631	18.30	0.000	2.754901	3.415922
PNIE						
exercise (Exercise vs Control)	9.932713	.2290178	43.37	0.000	9.483846	10.38158
TNDE						
exercise (Exercise vs Control)	3.174743	.1808011	17.56	0.000	2.820379	3.529107
TE						
exercise (Exercise vs Control)	13.10746	.2304752	56.87	0.000	12.65573	13.55918

Note: Outcome equation includes treatment-mediator interaction.

Auxiliary parameters

. mediate, equations

Causal mediation analysis Number of obs = 2,000

Outcome model: Linear
 Mediator model: Linear
 Mediator variable: bonotonin
 Treatment type: Binary

wellbeing	Coefficient	Robust std. err.	z	P> z	[95% conf. interval]
PCmeans					
Y0M0	58.89975	.228515	249.00	0.000	56.45187 57.34763
Y1M0	59.98516	.2555341	234.74	0.000	59.48432 60.486
Y0M1	66.83246	.2644294	252.74	0.000	66.31419 67.35073
Y1M1	70.0072	.2314185	302.51	0.000	69.55363 70.46077
NIE					
exercise (Exercise vs Control)					
	10.02204	.2256812	44.41	0.000	9.579717 10.46437
NDE					
exercise (Exercise vs Control)					
	3.085412	.168631	18.30	0.000	2.754901 3.415922
PNIE					
exercise (Exercise vs Control)					
	9.932715	.2290178	43.37	0.000	9.483846 10.38158
TNDE					
exercise (Exercise vs Control)					
	3.174743	.1808011	17.56	0.000	2.820379 3.529107
TE					
exercise (Exercise vs Control)					
	13.10746	.2304752	56.87	0.000	12.65573 13.55918
wellbeing					
exercise					
	2.777685	.6469446	4.31	0.000	1.513616 4.041753
bonotonin					
	-.2141319	.0026418	81.05	0.000	-.208954 -.2193099
c.bonotonin					
exercise#					
	.0019258	.0034941	0.55	0.582	-.0049224 .0087741
basewell					
	-.1685634	.0038294	44.02	0.000	-.1610579 -.1760689
age					
	-.0266714	.0072856	3.66	0.000	-.032392 -.0409509
gender					
	-.1031899	.1282411	-0.80	0.421	-.3545379 .1481581
hstatus					
	-.9787586	.0773014	12.66	0.000	-.8272506 -1.130267
_cons					
	9.508461	.5918832	16.06	0.000	8.348391 10.66853
bonotonin					
exercise					
	46.38595	.8963335	51.75	0.000	44.62916 48.14273
basebono					
	1.019825	.0154741	65.91	0.000	.9894966 1.050154
age					
	-.368765	.049656	7.43	0.000	-.271441 -.466089
gender					
	5.648102	.8946093	6.31	0.000	3.8947 7.401504
hstatus					
	3.662404	.5353618	6.84	0.000	2.613164 4.711743
_cons					
	-40.92391	3.646124	-11.22	0.000	-48.07018 -33.77764

Note: Outcome equation includes treatment-mediator interaction.

Binary outcome and mediator

```
. mediate (bwellbeing basewell age gender hstatus, logit)    ///  
> (bbonotonin basebono age gender hstatus, logit)         ///  
> (exercise), nointeraction
```

Iteration 0: EE criterion = 1.413e-18

Iteration 1: EE criterion = 1.371e-32

Causal mediation analysis

Number of obs = 2,000

Outcome model: Logit

Mediator model: Logit

Mediator variable: bbonotonin

Treatment type: Binary

bwellbeing	Robust				[95% conf. interval]	
	Coefficient	std. err.	z	P> z		
NIE						
exercise (Exercise vs Control)	.1053001	.0142631	7.38	0.000	.0773449	.1332553
NDE						
exercise (Exercise vs Control)	.1528838	.0189013	8.09	0.000	.115838	.1899296
TE						
exercise (Exercise vs Control)	.2581839	.014312	18.04	0.000	.2301328	.286235

Note: Outcome equation does not include treatment-mediator interaction.

Treatment effects as risk ratios

```
. estat rr
```

```
estat rr requires potential-outcome means; refitting model ...
```

```
Transformed treatment effects
```

```
Number of obs = 2,000
```

bwellbeing	Risk ratio	Robust std. err.	z	P> z	[95% conf. interval]	
NIE exercise (Exercise vs Control)	1.22985	.0383193	6.64	0.000	1.156993	1.307295
NDE exercise (Exercise vs Control)	1.500861	.0714322	8.53	0.000	1.367188	1.647603
TE exercise (Exercise vs Control)	1.845833	.0706637	16.01	0.000	1.712403	1.98966

Treatment effects as odds ratios

```
. estat or  
estat or requires potential-outcome means; refitting model ...
```

```
Transformed treatment effects Number of obs = 2,000
```

bwellbeing	Odds ratio	Robust std. err.	z	P> z	[95% conf. interval]	
NIE exercise (Exercise vs Control)	1.526485	.087768	7.36	0.000	1.363802	1.708575
NDE exercise (Exercise vs Control)	1.924312	.1529157	8.24	0.000	1.646777	2.248621
TE exercise (Exercise vs Control)	2.937434	.1841548	17.19	0.000	2.597791	3.321482

Example data (2)

```
. webuse birthweight
(Fictional birthweight data)

. list bweight ncigs college ses sespar age in 1/5, clean
```

	bweight	ncigs	college	ses	sespar	age
1.	3621	1	No	5.3581	3.308523	29
2.	3278	0	Yes	9.556957	4.376035	38
3.	3073	1	No	3.980829	6.580275	39
4.	3306	0	Yes	11.17643	12.12075	30
5.	4517	0	Yes	9.026146	4.738766	28

Exponential mean and Poisson models

```
. mediate (bweight sespar c.age##c.age, expmean) ///  
> (ncigs sespar c.age##c.age, poisson) ///  
> (college), nointeract
```

Iteration 0: EE criterion = 3.250e-13

Iteration 1: EE criterion = 9.147e-18

Causal mediation analysis

Number of obs = 2,000

Outcome model: Exponential mean

Mediator model: Poisson

Mediator variable: ncigs

Treatment type: Binary

		Robust				[95% conf. interval]	
bweight	Coefficient	std. err.	z	P> z			
NIE							
college (Yes vs No)	198.978	23.53279	8.46	0.000	152.8546	245.1014	
NDE							
college (Yes vs No)	320.3318	34.47792	9.29	0.000	252.7563	387.9072	
TE							
college (Yes vs No)	519.3098	28.70435	18.09	0.000	463.0503	575.5693	

Note: Outcome equation does not include treatment-mediator interaction.

Estimating incidence-rate ratios

```
. estat irr
```

```
estat irr requires potential-outcome means; refitting model ...
```

```
Transformed treatment effects
```

```
Number of obs = 2,000
```

bweight	Robust		z	P> z	[95% conf. interval]	
	IRR	std. err.				
NIE college (Yes vs No)	1.057819	.0072037	8.25	0.000	1.043794	1.072033
NDE college (Yes vs No)	1.102636	.0113921	9.46	0.000	1.080533	1.125192
TE college (Yes vs No)	1.16639	.009948	18.05	0.000	1.147055	1.186052

Estimating controlled direct effects

```
. estat cde, mvalue(0 1)
```

```
Controlled direct effect
```

```
Number of obs = 2,000
```

```
Mediator variable: ncigs
```

```
Mediator values:
```

```
1._at: ncigs = 0
```

```
2._at: ncigs = 1
```

	Delta-method		z	P> z	[95% conf. interval]	
	CDE	std. err.				
college@_at (Yes vs No)						
1 (Yes vs No)	341.955	35.26807	9.70	0.000	272.8308	411.0791
2	332.6419	34.94916	9.52	0.000	264.1428	401.141

Estimating differences between controlled direct effects

```
. estat cde, mvalue(0 1) contrast
```

```
Controlled direct effect
```

```
Number of obs = 2,000
```

```
Mediator variable: ncigs
```

```
Mediator values:
```

```
1._at: ncigs = 0
```

```
2._at: ncigs = 1
```

	Delta-method				
	CDE	std. err.	z	P> z	[95% conf. interval]
_at#college (2 vs 1) (Yes vs No)	-9.313066	.9748033	-9.55	0.000	-11.22365 -7.402487

More treatment interactions

```
. mediate (bweight sespar c.age##c.age)          ///
>         i.college#(c.sespar c.age##c.age), expmean)  ///
>         (ncigs c.sespar c.age##c.age)          ///
>         i.college#(c.sespar c.age##c.age), poisson)  ///
>         (college)
```

Iteration 0: EE criterion = 1.691e-12

Iteration 1: EE criterion = 1.122e-14

Causal mediation analysis

Number of obs = 2,000

Outcome model: Exponential mean

Mediator model: Poisson

Mediator variable: ncigs

Treatment type: Binary

bweight	Robust				
	Coefficient	std. err.	z	P> z	[95% conf. interval]
NIE college (Yes vs No)	111.6007	67.53715	1.65	0.098	-20.76971 243.971
NDE college (Yes vs No)	407.5962	72.49614	5.62	0.000	265.5063 549.686
TE college (Yes vs No)	519.1968	28.71853	18.08	0.000	462.9095 575.4841

Note: Outcome equation includes treatment-mediator interaction.

Mediator interactions

```
. mediate (bweight sespar c.age##c.age                ///
>          c.ncigs#(c.sespar c.age##c.age), expmean)  ///
>          (ncigs c.sespar c.age##c.age, poisson)     ///
>          (college)
```

Iteration 0: EE criterion = 6.460e-11

Iteration 1: EE criterion = 5.837e-15

Causal mediation analysis

Number of obs = 2,000

Outcome model: Exponential mean

Mediator model: Poisson

Mediator variable: ncigs

Treatment type: Binary

		Robust				
bweight		Coefficient	std. err.	z	P> z	[95% conf. interval]
NIE	college					
(Yes vs No)		86.26849	68.96645	1.25	0.211	-48.90328 221.4403
NDE	college					
(Yes vs No)		431.5822	73.70305	5.86	0.000	287.1269 576.0375
TE	college					
(Yes vs No)		517.8507	28.64809	18.08	0.000	461.7015 573.9999

Note: Outcome equation includes treatment-mediator interaction.

Multivalued treatment

```
. mediate (wellbeing age gender i.hstatus basewell)    ///
>          (bonotonin basebono)                    ///
>          (mexercise)                             ///
```

Iteration 0: EE criterion = 1.778e-27

Iteration 1: EE criterion = 1.198e-27

Causal mediation analysis Number of obs = 2,000

Outcome model: Linear

Mediator model: Linear

Mediator variable: bonotonin

Treatment type: Multivalued

wellbeing	Coefficient	Robust std. err.	z	P> z	[95% conf. interval]	
NIE						
mexercise						
(45 minutes						
vs						
Control)	5.128899	.3505171	14.63	0.000	4.441898	5.815899
(90 minutes						
vs						
Control)	9.780537	.2880877	33.95	0.000	9.215895	10.34518
NDE						
mexercise						
(45 minutes						
vs						
Control)	1.197498	.1750038	6.84	0.000	.8544965	1.540499
(90 minutes						
vs						
Control)	3.051084	.2071236	14.73	0.000	2.645129	3.457039
TE						
mexercise						
(45 minutes						
vs						
Control)	6.326396	.3894269	16.25	0.000	5.563134	7.089659
(90 minutes						
vs						
Control)	12.83162	.2967962	43.23	0.000	12.24991	13.41333

Note: Outcome equation includes treatment-mediator interaction.

Continuous treatment

```
. webuse birthweight
(Fictional birthweight data)

. qui sum ses

. generate std_ses = (ses-r(mean))/r(sd)

. mediate (bweight sespar c.age##c.age, expmean) ///
> (ncigs sespar c.age##c.age, poisson) ///
> (std_ses, continuous(0 2)), nointeract
```

Iteration 0: EE criterion = 1.470e-12

Iteration 1: EE criterion = 1.816e-17

Causal mediation analysis

Number of obs = 2,000

Outcome model: Exponential mean

Mediator model: Poisson

Mediator variable: ncigs

Treatment type: Continuous

Continuous treatment levels:

0: std_ses = 0 (control)

1: std_ses = 2

		Robust				[95% conf. interval]	
	bweight	Coefficient	std. err.	z	P> z		
NIE							
	std_ses (1 vs 0)	110.1346	8.724232	12.62	0.000	93.03538	127.2337
NDE							
	std_ses (1 vs 0)	180.0172	34.77372	5.18	0.000	111.8619	248.1724
TE							
	std_ses (1 vs 0)	290.1517	33.85571	8.57	0.000	223.7958	356.5077

Note: Outcome equation does not include treatment-mediator interaction.

Continuous treatment with multiple evaluation points

```
. mediate (bweight sespar c.age#c.age, expmean) ///
>         (ncigs sespar c.age#c.age, poisson)    ///
>         (std_ses, continuous(0 -2 -1 1 2)), nointeract
```

Iteration 0: EE criterion = 1.470e-12

Iteration 1: EE criterion = 2.374e-17

Causal mediation analysis

Number of obs = 2,000

Outcome model: Exponential mean

Mediator model: Poisson

Mediator variable: ncigs

Treatment type: Continuous

Continuous treatment levels:

0: std_ses = 0 (control)

1: std_ses = -2

2: std_ses = -1

3: std_ses = 1

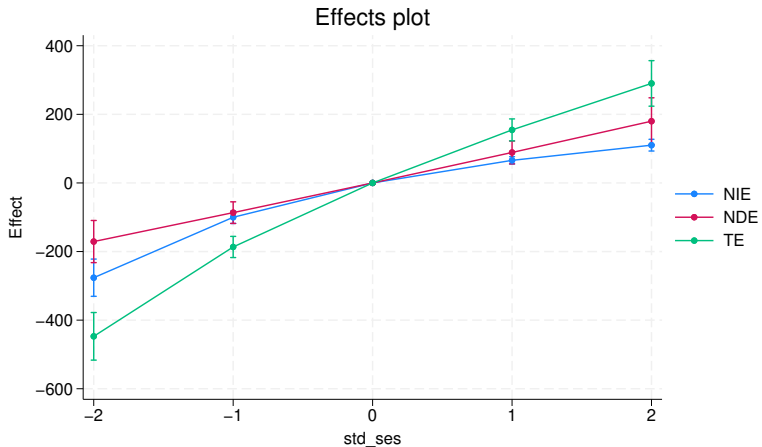
4: std_ses = 2

		Robust				
bweight		Coefficient	std. err.	z	P> z	[95% conf. interval]
NIE						
std_ses						
(1 vs 0)		-276.2757	27.69004	-9.98	0.000	-330.5471 -222.0042
(2 vs 0)		-100.1155	9.170566	-10.92	0.000	-118.0894 -82.14148
(3 vs 0)		65.84585	5.423096	12.14	0.000	55.21678 76.47493
(4 vs 0)		110.1346	8.724232	12.62	0.000	93.03538 127.2337
NDE						
std_ses						
(1 vs 0)		-170.9012	31.33649	-5.45	0.000	-232.3196 -109.4828
(2 vs 0)		-86.56069	16.08129	-5.38	0.000	-118.0794 -55.04193
(3 vs 0)		88.83929	16.94031	5.24	0.000	55.6369 122.0417
(4 vs 0)		180.0172	34.77372	5.18	0.000	111.8619 248.1724
TE						
std_ses						
(1 vs 0)		-447.1769	35.41401	-12.63	0.000	-516.5871 -377.7667
(2 vs 0)		-186.6761	15.73291	-11.87	0.000	-217.5121 -155.8402
(3 vs 0)		154.6851	16.31969	9.48	0.000	122.6991 186.6712
(4 vs 0)		290.1517	33.85571	8.57	0.000	223.7958 356.5077

Note: Outcome equation does not include treatment-mediator interaction.

```
. estat effectplot
```

Plotting treatment effects



Final remarks

- Learn more:

<https://www.stata.com/manuals/causalmediate.pdf>

Thank you!